



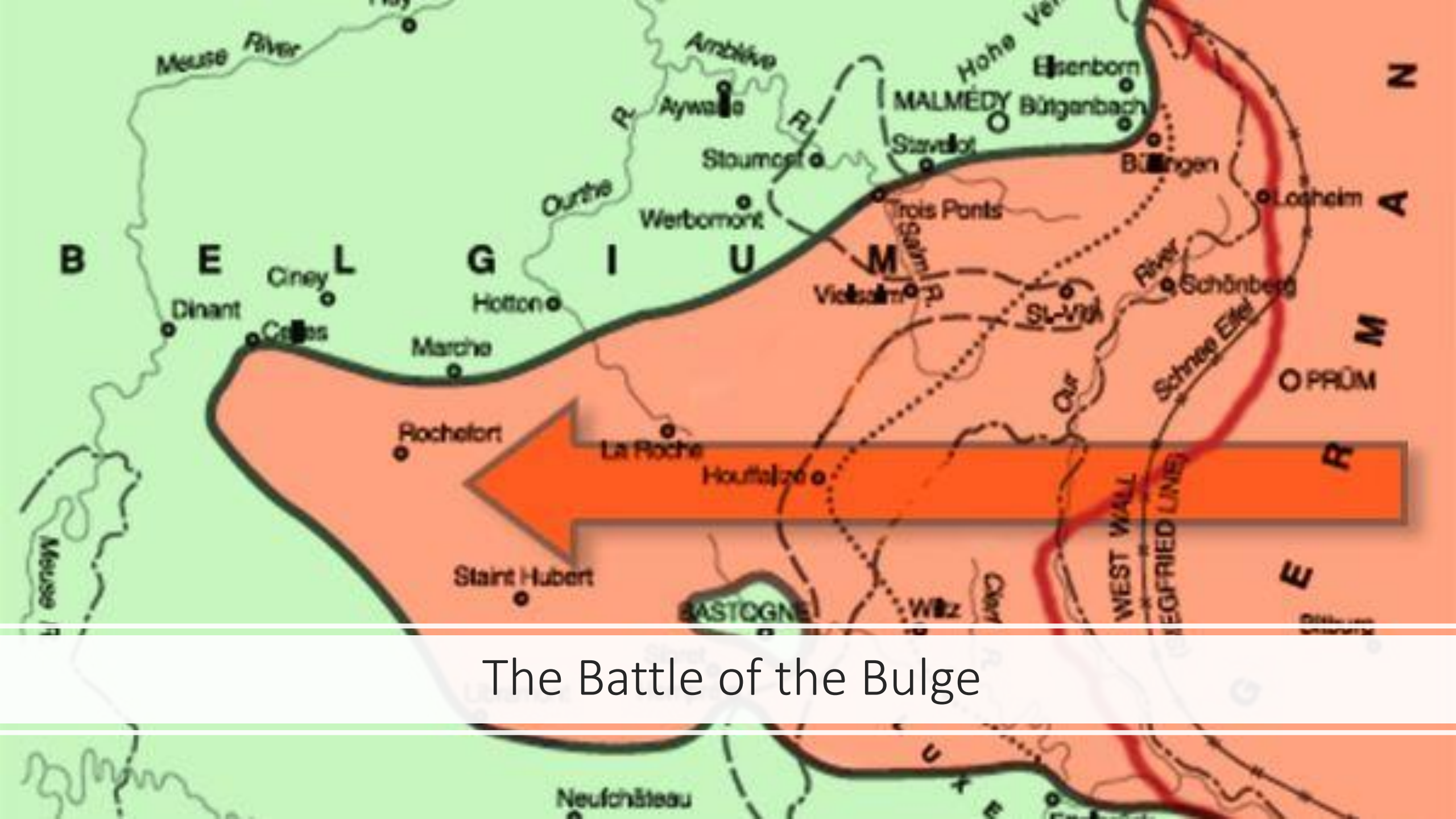
Rrrrrr Shivers me Timber  
Its Rrrrr time for some  
Ere Rrrrrr

MATH 4753



© 1998

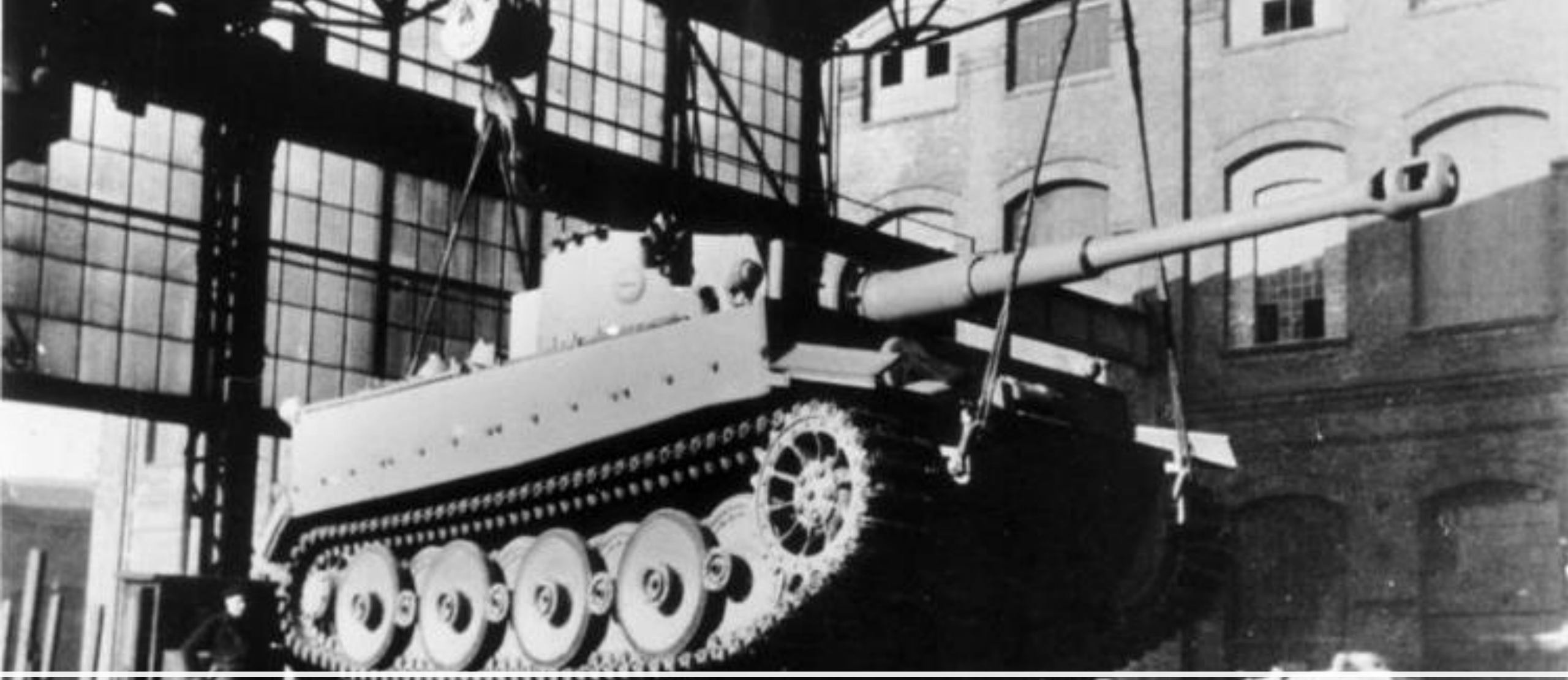




The Battle of the Bulge



Tiger 2



Where were the tanks made?



The Tiger I and Tiger II tanks were primarily manufactured at the Henschel factory in Kassel, Germany.

# Serial numbers



# Classical

# Bayesian

1,2,3,...,N

Tanks left after  
a battle

$$\hat{N} = m + \frac{m}{k} - 1$$

$$\hat{N} = \frac{(m-1)(k-1)}{k-2}$$

3,8,18,50

$m = \max(\text{sample}), k = \text{sample size}$

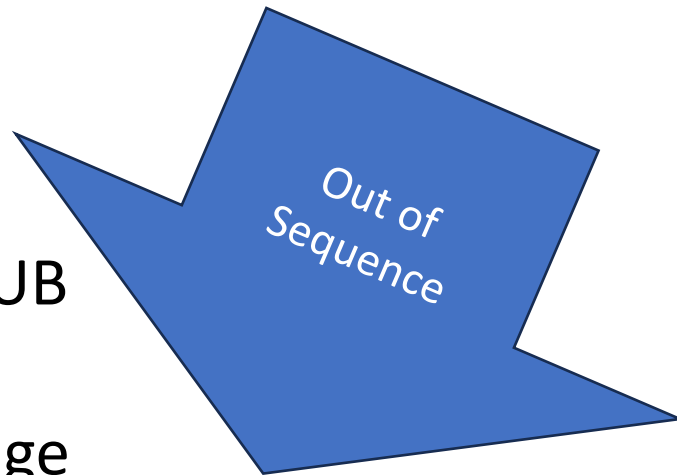
# How did the estimation go?

Estimates for some specific months are given as:<sup>[7]</sup>

<b>Month</b>	<b>Statistical estimate</b>	<b>Intelligence estimate</b>	<b>German records</b>
June 1940	169	1,000	122
June 1941	244	1,550	271
August 1942	327	1,550	342

# Today (Possibly)

1. Introduce the course
2. Canvas
3. Syllabus
4. Expectations
5. GIT and GITHUB
6. Clone Intro2R
7. Make R package
8. Lab 1 (Lab order 1,2,3,4,5,6,7,)
9. Chapters 1 and 2 (possibly)



# Chapter 1

---

Dr. Wayne Stewart



# **STATISTICS**

for Engineering and the Sciences

**SIXTH EDITION**



Make sure  
you do the  
quiz

Differences between  
measurements, true  
zero exists

**Ratio Data**

Quantitative Data

Differences between  
measurements but no  
true zero

**Interval Data**

Ordered Categories  
(rankings, order, or  
scaling)

**Ordinal Data**

Qualitative Data

Categories (no  
ordering or direction)

**Nominal Data**



# Chapter 1

## Introduction

**“The role of statistics in data analysis”**

## OBJECTIVE

*To identify the role of statistics in the analysis of data from engineering and the sciences*

## CONTENTS

- 1.1 Statistics: The Science of Data
- 1.2 Fundamental Elements of Statistics
- 1.3 Types of Data
- 1.4 Collecting Data: Sampling
- 1.5 The Role of Statistics in Critical Thinking
- 1.6 A Guide to Statistical Methods Presented in This Text

- *STATISTICS IN ACTION*
- DDT Contamination of Fish in the Tennessee River

## **Definition 1.1**

**Statistics** is the science of data. This involves collecting, classifying, summarizing, organizing, analyzing, and interpreting data.



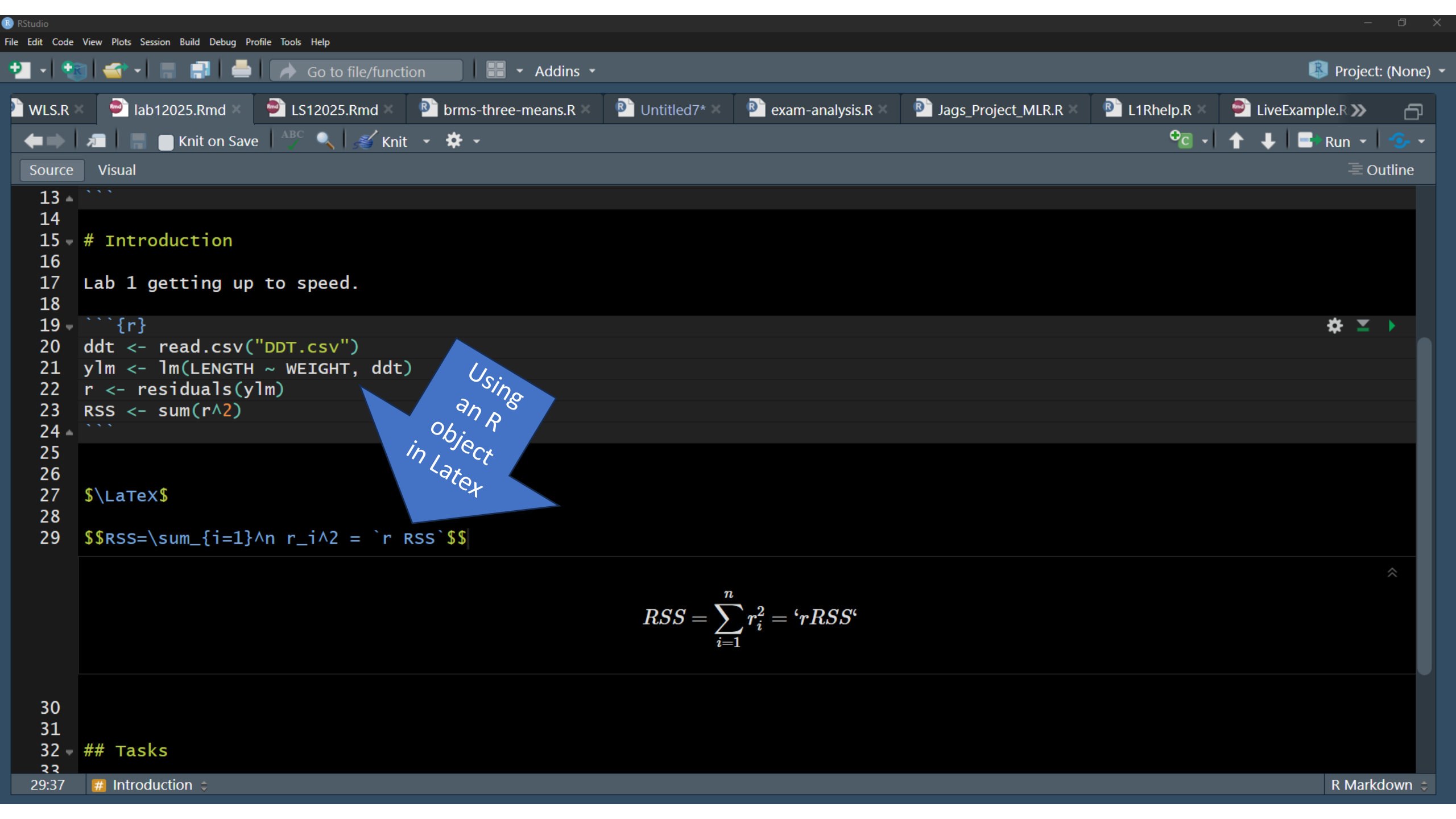
—

You will need to be  
“competent” in R

---

- This means for this course that you will need to understand
  - Vectors
  - Matrices
  - Data frames
  - Subsetting
  - Assignment
  - Creating Functions
  - Plotting
    - Base R
    - Ggplot





```
13  ```
14
15  # Introduction
16
17  Lab 1 getting up to speed.
18
19  ```{r}
20  ddt <- read.csv("DDT.csv")
21  ylm <- lm(LENGTH ~ WEIGHT, ddt)
22  r <- residuals(ylm)
23  RSS <- sum(r^2)
24  ```
25
26
27   $\LaTeX$ 
28
29   $RSS = \sum_{i=1}^n r_i^2 = 'rRSS'$ 
```

Using an R object in Latex

$$RSS = \sum_{i=1}^n r_i^2 = 'rRSS'$$

```
30
31
32  ## Tasks
33
```

## Introduction

## Tasks

Dr. Wayne Stewart

2025-01-15

# Introduction

Lab 1 getting up to speed.

```
ddt <- read.csv("DDT.csv")
ylm <- lm(LENGTH ~ WEIGHT, ddt)
r <- residuals(ylm)
RSS <- sum(r^2)
```

*L<sup>A</sup>T<sub>E</sub>X*

$$RSS = \sum_{i=1}^n r_i^2 = 3870.625477$$

## Tasks

### Task 1

```
getwd()
```

```
## [1] "D:/2023-MATH4753/Laboratories/Lab1Rmd"
```

# Make sure you clone package “Intro2R”

The screenshot shows a web browser window displaying a Canvas LMS page. The browser's address bar shows the URL: `canvas.ou.edu/courses/173917/pages/install-source-files-from-github`. The page title is "MATH-4753-12-2020-FALL > Pages > Install source files from GITHUB".

On the left side, there is a navigation sidebar with icons for Account, Dashboard, Courses, Calendar, Inbox (with a notification badge of 257), and Commons. Below the sidebar, a taskbar shows "Rtools35 (2).exe" with a "Canceled" status.

The main content area of the page includes:



- A breadcrumb trail: [MATH-4753-12-2020-FALL](#) > [Pages](#) > Install source files from GITHUB
- A "Fall 2020" label.
- Action buttons: "View All Pages", "Published" (with a green checkmark), "Edit", "Immersive Reader", and a menu icon.
- A list of navigation links: [Home](#), [Announcements](#), [Assignments](#), [Discussions](#), [Grades](#), [People](#), [Pages](#) (highlighted), [Files](#), and [Syllabus](#).
- The main heading: "Install source files from GITHUB"
- The main text: "Obtaining the latest files from GITHUB and then creating a local package is a great way to learn package making and also learn R in general." followed by "Please follow the steps below to install all source files for **Intro2R**".
- A sub-heading: "Please follow the instructions here:"
- A link: [project.html](#)

At the bottom right of the page, there is a "Show all" button.




## Install my package

```
devtools::install_github("https://github.com/MATHSTAT  
SOU/Intro2R.git", build_vignettes = TRUE, force =  
TRUE)
```

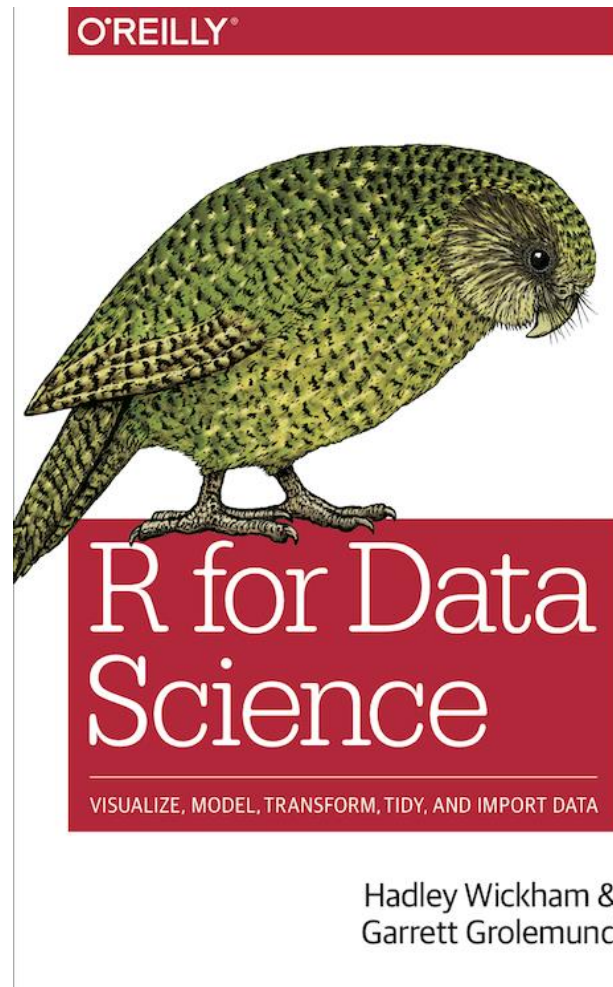


The science of statistics is commonly applied to two types of problems:

1. Summarizing, describing, and exploring data
  2. Using sample data to infer the nature of the data set from which the sample was selected
- 

Plenty of  
resources –  
mostly labs!!

Free books



R Programming  
for Data Science



Roger D. Peng

<https://bookdown.org/>

Addins
Project: (None)

nultinom.stan
lab1 (1).R
template.Rmd
lab1test2.Rmd\*

Knit on Save
Knit
Run

Source
Visual
Outline

```

1 ---
2 title: "Template"
3 author: "Dr Wayne Stewart"
4 date: "`r Sys.Date()`"
5 output:
6   html_document:
7     toc: yes
8     toc_float: yes
9 ---
10
11

```

6:17 # Template R Markdown

Console

Environment

318

R Global Environment

Data

ddt
144...

Values

Files Plots

Install
Update

N De...

User Library

Com
  
 Multi



New 2024 and  
continues this  
semester.  
Bayesian STATS  
using STAN

<https://canvas.ou.edu/courses/222644/pages/help>

# You will learn the basic Bayesian Algorithm

Bayesian computation: MATH-4753-2-3-spring-2022 - Google Chrome

canvas.ou.edu/courses/222644/pages/bayesian-computation

MATH-4753-2-3-spring-2022 > Pages > Bayesian computation

View All Pages

## Bayesian computation

### Introduction

We will use STAN to write our Bayesian models. The code will then be converted to C++ compiled into an executable and then run. For good examples of use see the following link [download the pdf](#) and also <https://mc-stan.org/users/documentation/>

### Installing STAN

We will be using the R package "rstan" to interact with stan. Please use the following link to get the latest information <https://mc-stan.org/users/interfaces/rstan.html>

### Bayesian modeling

All Bayesian modeling MUST instantiate Bayes' formula

$$p(\theta, X) \propto p(\theta) f(X|\theta)$$

In other words, every Bayesian model must have:

- Data  $X$
- Parameters or parameter vector  $\theta$
- a Prior density is usually expressed as the product of the marginals  $p(\theta) = p_1(\theta_1) \times \dots \times p_k(\theta_k)$
- a likelihood function  $f(X|\theta)$  - this will also be expressed assuming independence within the structure of the data

This will define the posterior  $p(\theta, X)$  from which we will create posterior samples of the parameters.

Almost analogous to this STAN creates a model with a template:

```
data{  
  parameters{  
    model{
```

We will look at a basic example to see how the syntax goes.

### Example 1: Estimating the mean from a single sample

Suppose we wish to model the length of fish caught in the Tennessee river using a normal distribution where we do not know the population mean but do know the standard deviation to be 7.

Then a Bayesian approach would be to recognize "mu" to be the unknown parameter (theta above) and ddsLENGTH to be the vector of sampled data. We will use "y" in the model for the length.


You must create a stan file into which the template goes:

```
data {  
  int<lower=0> N;  
  vector[N] ys;  
}
```



## Definition 1.2

The branch of statistics devoted to the organization, summarization, and description of data sets is called **descriptive statistics**.





### **Definition 1.3**

The branch of statistics concerned with using sample data to make an inference about a large set of data is called **inferential statistics**.



### **Definition 1.4**

A statistical **population** is a data set (usually large, sometimes conceptual) that is our target of interest.


### **Definition 1.5**

A **sample** is a subset of data selected from the target population.



### **Definition 1.6**


The object (e.g., person, thing, transaction, specimen, or event) upon which measurements are collected is called the **experimental unit**. (*Note: A population consists of data collected on many experimental units.*)





## **Definition 1.7**


A **variable** is a characteristic or property of an individual experimental unit.









### **Definition 1.8**


A **measure of reliability** is a statement (usually quantified) about the degree of uncertainty associated with a statistical inference.







## Four Elements of Descriptive Statistical Problems

1. The population or sample of interest
  2. One or more variables (characteristics of the population or sample units) that are to be investigated
  3. Tables, graphs, or numerical summary tools
  4. Identification of patterns in the data
- 
- 



## Five Elements of Inferential Statistical Problems

1. The population of interest
  2. One or more variables (characteristics of the experimental units) that are to be investigated
  3. The sample of experimental units
  4. The inference about the population based on information contained in the sample
  5. A measure of reliability for the inference
- 
- 



# Types of Data




### **Definition 1.9**

**Quantitative data** are those that are recorded on a naturally occurring numerical scale, i.e., they represent the quantity or amount of something.

### **Definition 1.10**

**Qualitative data** are those that cannot be measured on a natural numerical scale, i.e., they can only be classified into categories.



\*A finer breakdown of data types into nominal, ordinal, interval, and ratio data is possible. **Nominal** data are qualitative data with categories that cannot be meaningfully ordered. **Ordinal** data are also qualitative data, but a distinct ranking of the groups from high to low exists. **Interval** and **ratio** data are two different types of quantitative data. For most statistical applications (and all the methods presented in this introductory text), it is sufficient to classify data as either quantitative or qualitative.



For our purposes!!



Learn more about the difference between nominal, ordinal, interval and ratio data with this video by [NurseKillam](#)

OK to compute....	Nominal	Ordinal	Interval	Ratio
Frequency distribution	Yes	Yes	Yes	Yes
Median and percentiles	No	Yes	Yes	Yes
Add or subtract	No	No	Yes	Yes
Mean, standard deviation, standard error of the mean	No	No	Yes	Yes
Ratios, coefficient of variation	No	No	No	Yes

## Does measurement scale matter for data analysis?

Knowing the measurement scale for your variables can help prevent mistakes like taking the average of a group of zip (postal) codes, or taking the ratio of two pH values. Beyond that, knowing the measurement scale for your variables doesn't really help you plan your analyses or interpret the results.

Note that sometimes, the measurement scale for a variable is not clear cut. What kind of variable is color? In a psychological study of perception, different colors would be regarded as nominal. In a physics study, color is quantified by wavelength, so color would be considered a ratio variable. What about counts?

# Sampling

Once you decide on the type of data—quantitative or qualitative—appropriate for the problem at hand, you'll need to collect the data. Generally, you can obtain the data in three different ways:

1. Data from a *published source*
2. Data from a *designed experiment*
3. Data from an *observational study* (e.g., a *survey*)

### **Definition 1.11**

A **designed experiment** is a data-collection method where the researcher exerts full control over the characteristics of the experimental units sampled. These experiments typically involve a group of experimental units that are assigned the *treatment* and an untreated (or, *control*) group.

### **Definition 1.12**



An **observational study** is a data-collection method where the experimental units sampled are observed in their natural setting. No attempt is made to control the characteristics of the experimental units sampled. (Examples include *opinion polls* and *surveys*.)

### **Definition 1.11**

A **designed experiment** is a data-collection method where the researcher exerts full control over the characteristics of the experimental units sampled. These experiments typically involve a group of experimental units that are assigned the *treatment* and an untreated (or, *control*) group.


### **Definition 1.12**


An **observational study** is a data-collection method where the experimental units sampled are observed in their natural setting. No attempt is made to control the characteristics of the experimental units sampled. (Examples include *opinion polls* and *surveys*.)



**Definition 1.13**


A **representative sample** exhibits characteristics typical of those possessed by the population of interest.





**Definition 1.14**

A **simple random sample** of  $n$  experimental units is a sample selected from the population in such a way that every different sample of size  $n$  has an equal chance of selection.



```
> choose(100, 5) [1] 75287520
```

### Example 1.3

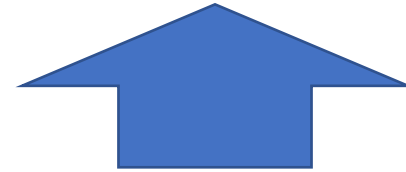
Obtaining a Simple Random Sample for Strength Testing

Suppose you want to randomly sample 5 glass-fiber strips from a lot of 100 strips for strength testing. (Note: In Chapter 3 we demonstrate that there are 75,287,520 possible samples that could be selected.) Use a random number generator to select a simple random sample of 5 glass-fiber strips.

```
> sample(1:100, 5, replace = FALSE)
[1] 43 75 58 55 28
```

Simple Random Sampling

In addition to simple random samples, there are more complex random sampling designs that can be employed. These include (but are not limited to) **stratified random sampling**, **cluster sampling**, and **systematic sampling**.

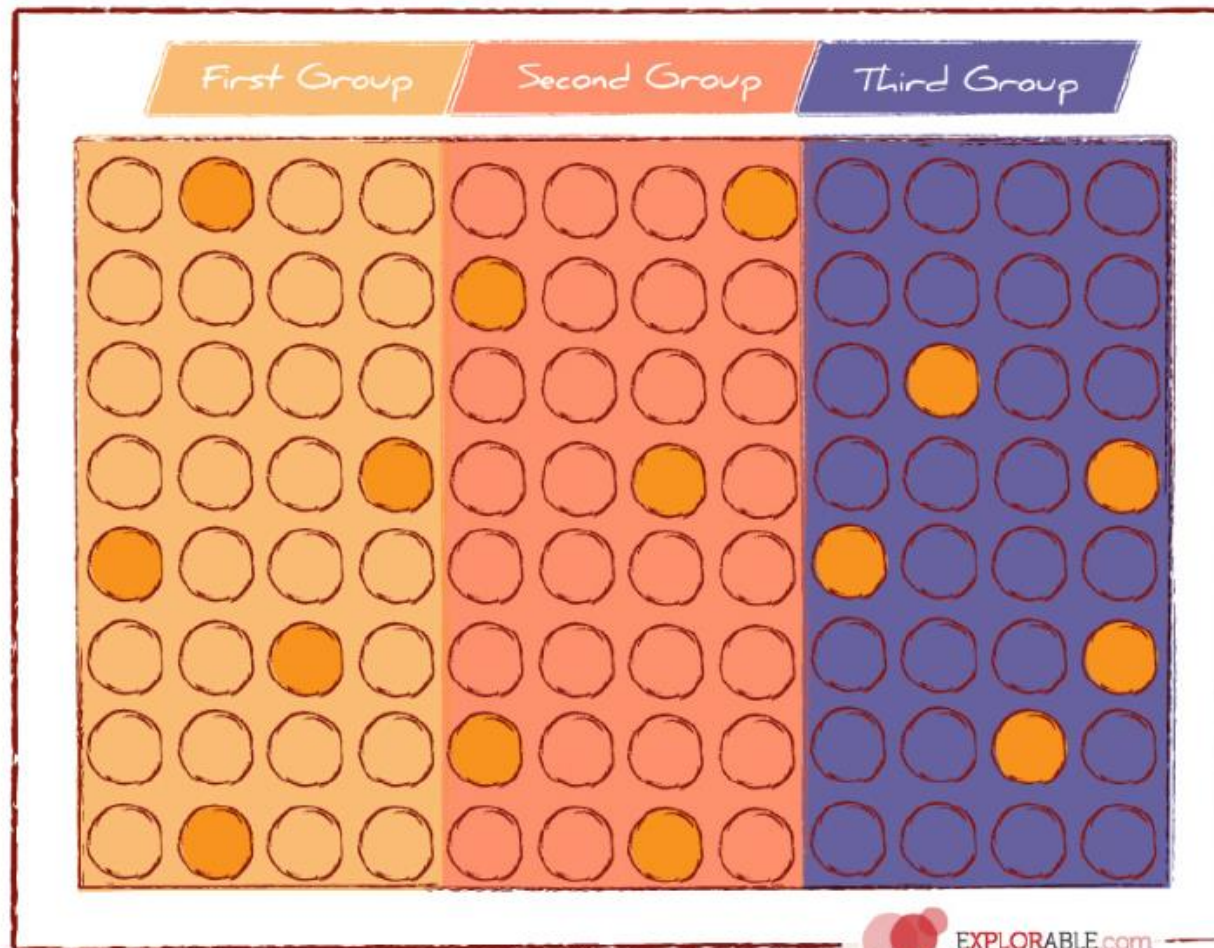


Choose every  $k$ th value

Random Sampling Designs

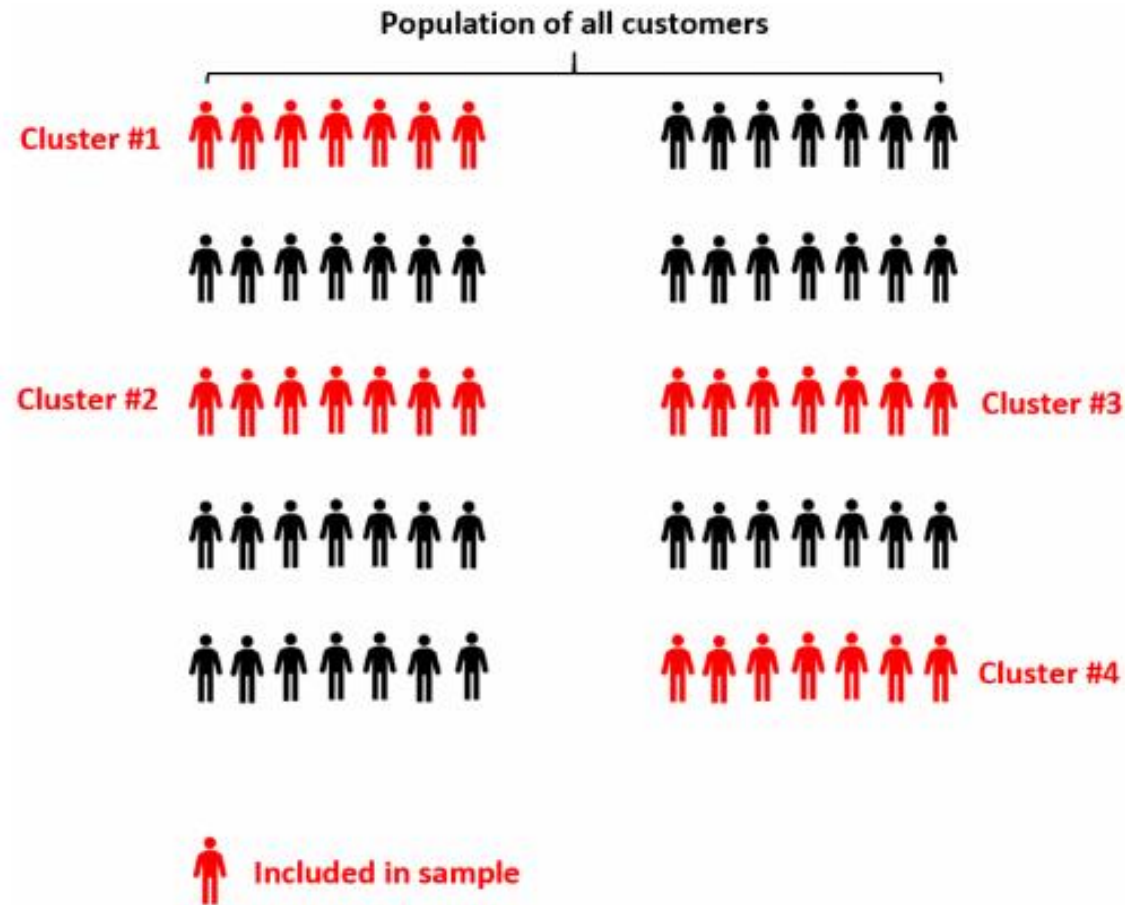
# Stratified Sampling

Stratified sampling is a probability sampling technique wherein the researcher divides the entire population into different subgroups or strata, then randomly selects the final subjects proportionally from the different **strata**.

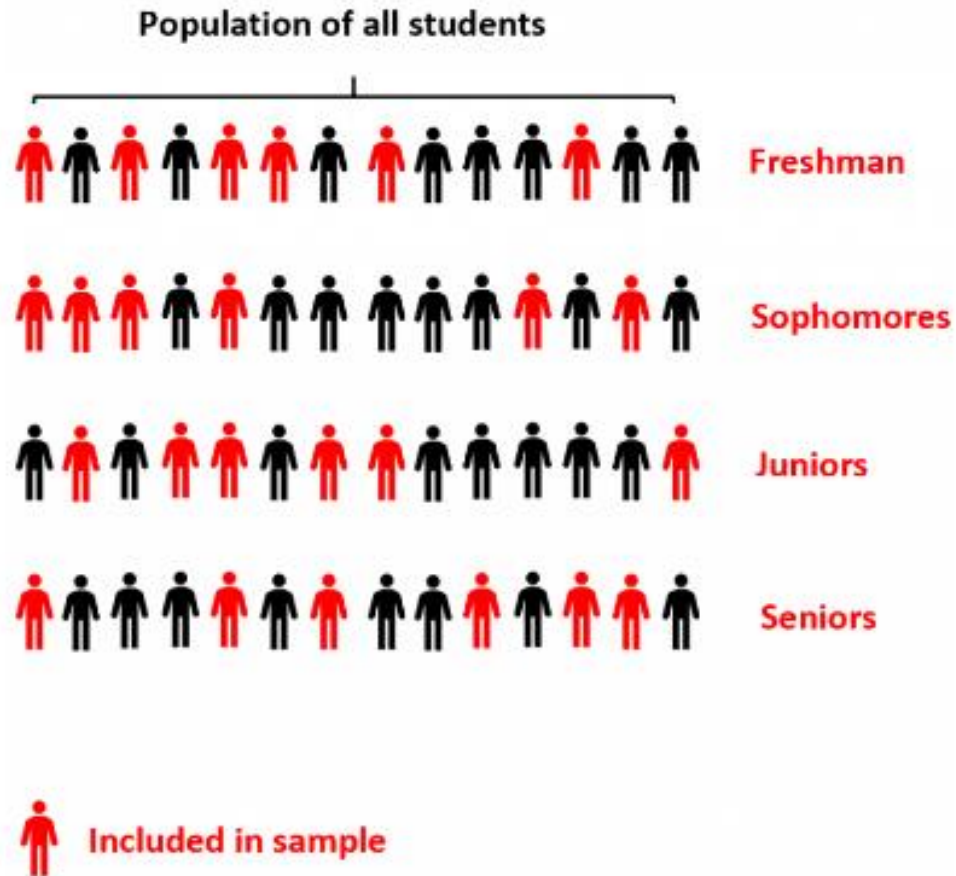


# Cluster sampling

<https://www.statology.org/cluster-sampling-vs-stratified-sampling/>



# Stratified sampling



# Required R skills

Data  
wrangling



Plotting





Example of  
sampling:  
Swiss  
municipalities



swissmunicipalities {sampling}

R Documentation

# The Swiss municipalities population

## Description

This population provides information about the Swiss municipalities in 2003.

## Usage

```
data(swissmunicipalities)
```

## Format

A data frame with 2896 observations on the following 22 variables:

CT

Swiss canton.

REG

Swiss region.

COM

municipality number.

Nom

municipality name.

A black and white photograph of a typewriter keyboard. The keys are arranged in a standard QWERTY layout. The text "Cluster sampling" is overlaid in white, centered horizontally across the middle of the keyboard. The lighting is dramatic, highlighting the metallic surfaces of the keys and the mechanical parts of the typewriter against a dark background.

# Cluster sampling

RStudio

File Edit Code View Plots Session Build Debug Profile Tools Help

Go to file/function Addins Project: (None)

Questions-answers-2022.Rmd vaers\_analysis.R suitability.Rmd Untitled12\* glm-table.R ch11-lda.R sampling.R\* swiss1

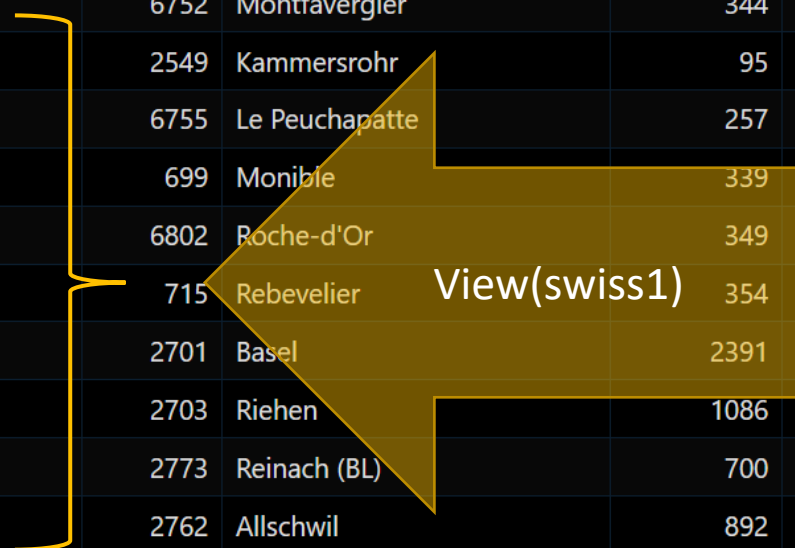
Filter

	CT	REG	COM	Nom	HApoly	Surfacesbois	Surfacescult	Alp	Airbat	Airind	P00BMTOT	P00BWTOT	Pop020
1	1	4	261	Zurich	8781	2326	967	0	2884	260	175836	187437	5732
2	25	1	6621	Geneve	1593	67	31	0	773	60	83449	94515	3242
3	12	3	2701	Basel	2391	97	93	0	1023	213	78736	87822	2816
4	2	2	351	Bern	5162	1726	1041	0	1070	212	59727	68907	1939
5	22	1	5586	Lausanne	4136	1635	714	0	856	64	58621	66293	2429
6	1	4	230	Winterthur	6787	2807	1827	0	972	238	43788	46695	1894
7	17	5	3203	St.Gallen	3940	1139	1222	0	812	134	34987	37639	1433
8	3	6	1061	Luzern	1581	408	183	0	524	27	27324	32172	953
9	2	2	371	Biel (BE)	2123	976	196	18	463	108	23447	25208	912
10	2	2	942	Thun	2158	425	694	0	523	137	19071	21306	812
11	2	2	355	Koniz	5099	1567	2621	0	515	53	17952	19830	786
12	24	2	6421	La Chaux-de-Fonds	5566	1572	2221	867	467	56	17535	19481	831
13	10	2	2196	Fribourg	930	164	138	0	301	40	16980	18567	686
14	14	5	2939	Schaffhausen	3102	1467	643	0	467	115	16026	17602	695
15	18	5	3901	Chur	2809	1456	477	49	354	82	15683	17306	688
16	24	2	6458	Neuchatel	1810	998	197	7	323	26	15542	17372	635

Showing 1 to 16 of 2,896 entries, 22 total columns

Untitled1 x sampling.R x swiss1 x

	CT	REG	COM	Nom	HApoly	Surfacesbois	Surfacescult	Alp	Airbat	Airind	P00BMTOT	P00BWTOT	Pop
2868	26	2	6752	Montfavergier	344	151	120	67	3	0	20	25	
2874	11	2	2549	Kammersrohr	95	37	55	0	1	0	21	18	
2876	26	2	6755	Le Peuchapatte	257	91	121	32	4	0	20	18	
2882	2	2	699	Monible	339	169	123	39	2	0	20	15	
2888	26	2	6802	Roche-d'Or	349	145	86	105	4	0	16	17	
2892	2	2	715	Rebevelier	354	142	104	107	1	0	19	11	
3	12	3	2701	Basel	2391	97	93	0	1023	213	78736	87822	
30	12	3	2703	Riehen	1086	276	283	0	302	2	9467	10903	
35	13	3	2773	Reinach (BL)	700	118	201	0	221	29	8911	9412	
36	13	3	2762	Allschwil	892	242	273	0	189	42	8714	9417	
38	19	3	4045	Wettingen	1062	415	228	0	230	17	8738	9132	
46	13	3	2770	Muttenz	1664	679	272	0	239	136	8120	8534	
50	19	3	4021	Baden	1318	752	132	0	227	40	8149	8121	
60	19	3	4001	Aarau	892	302	56	0	278	37	7374	8096	



Showing 1,496 to 1,510 of 2,896 entries, 22 total columns

Source



Console

Terminal

Background Jobs



R 4.1.2 · D:/RPACKAGES/Intro2MVS/

```

> # cluster sampling
> library(Intro2R)
> library(dplyr)
> library(ggplot2)
> library(sampling)
>
> data("swissmunicipalities") # bring in the data from the package
> swiss1 <- swissmunicipalities %>% mutate(REG = factor(REG)) #
  remake REG as a factor
> c1 <- sampling::cluster(data = swiss1, # invoke the cluster fu
  nction from the package sampling (::)
  +       clustertype = "REG",
  +       size = 3,
  +       method = "srswor",
  +       description = TRUE)
Number of selected clusters: 3
Number of units in the population and number of selected units:
2896 1381
>
> g <- ggplot(swiss1) # use ggplot layers to construct plot
> g <- g + geom_boxplot(aes(x = REG, y = Airbat, fill = REG)) #
  add boxplot layer
> g <- g + theme(legend.position = "bottom") # add a theme modi
  fication
> g # print the plot object

```

Environment

History

Connections

Build

Git

Tutorial



Files

Plots

Packages

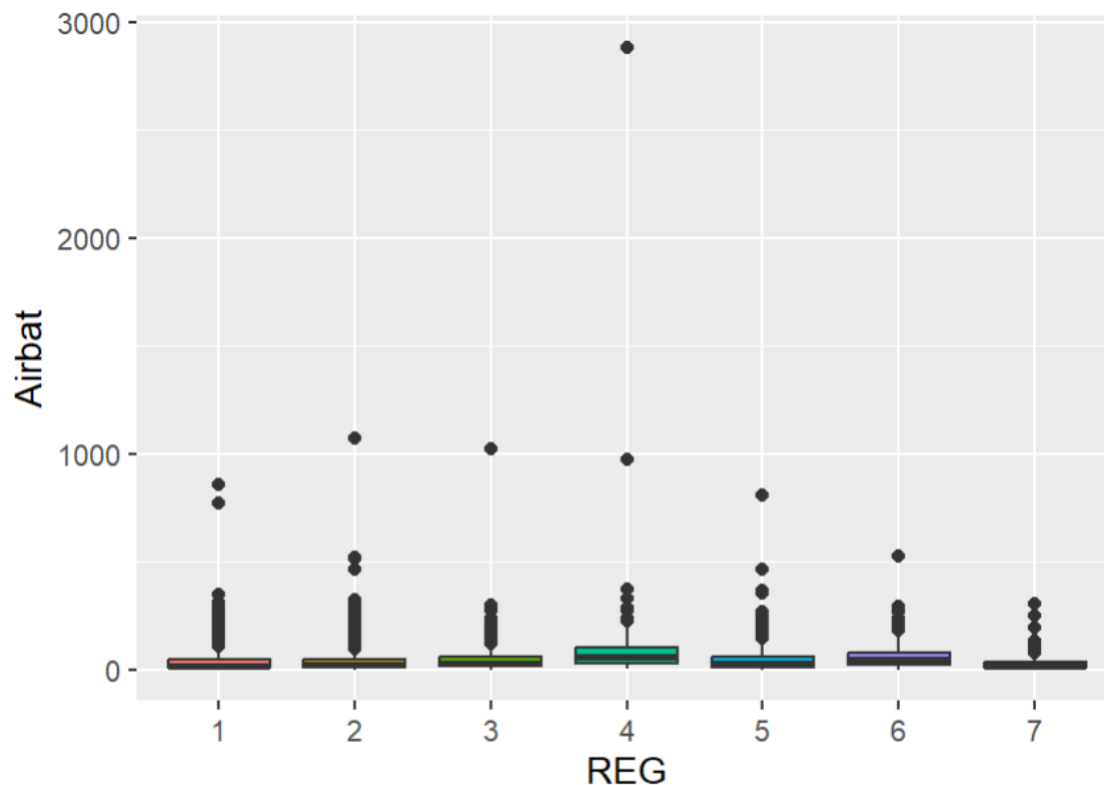
Help

Viewer

Presentation

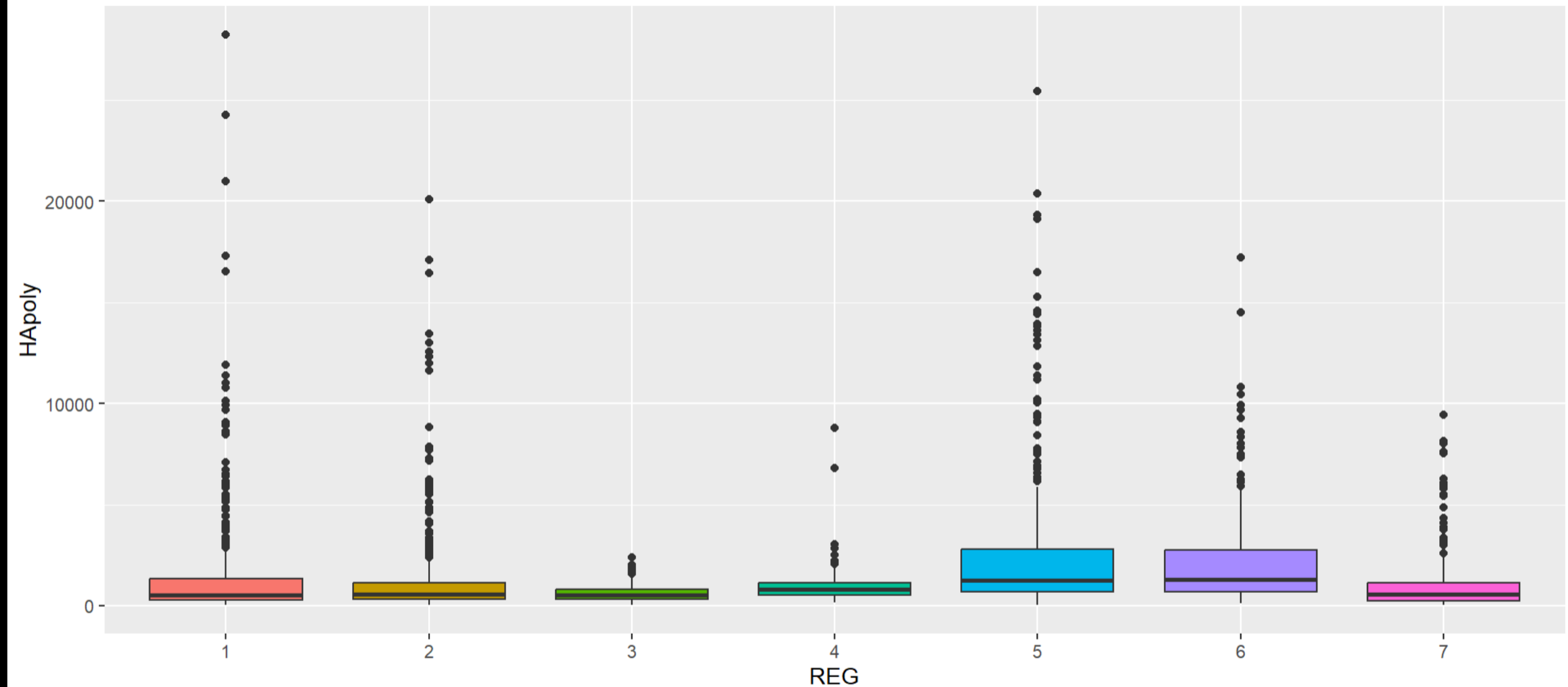


Zoom Export



REG

	1		3		5		7
	2		4		6		



Source

Console

Terminal

Background Jobs

R 4.1.2 · D:/RPACKAGES/Intro2MVS/

```
> 3/7 # proportion of categories selected
[1] 0.4285714
> data <- getdata(swiss1, c1)
> data2 <- within(data, REG <- factor(REG)) # a different way to r
eform REG as a factor
> g <- ggplot(data2, aes(x = REG, y = Airbat, fill = REG))
> g <- g + geom_boxplot()
> g <- g + theme( legend.position = "bottom" )
> g
> |
```

Environment

History

Connections

Build

Git

Tutorial

Files

Plots

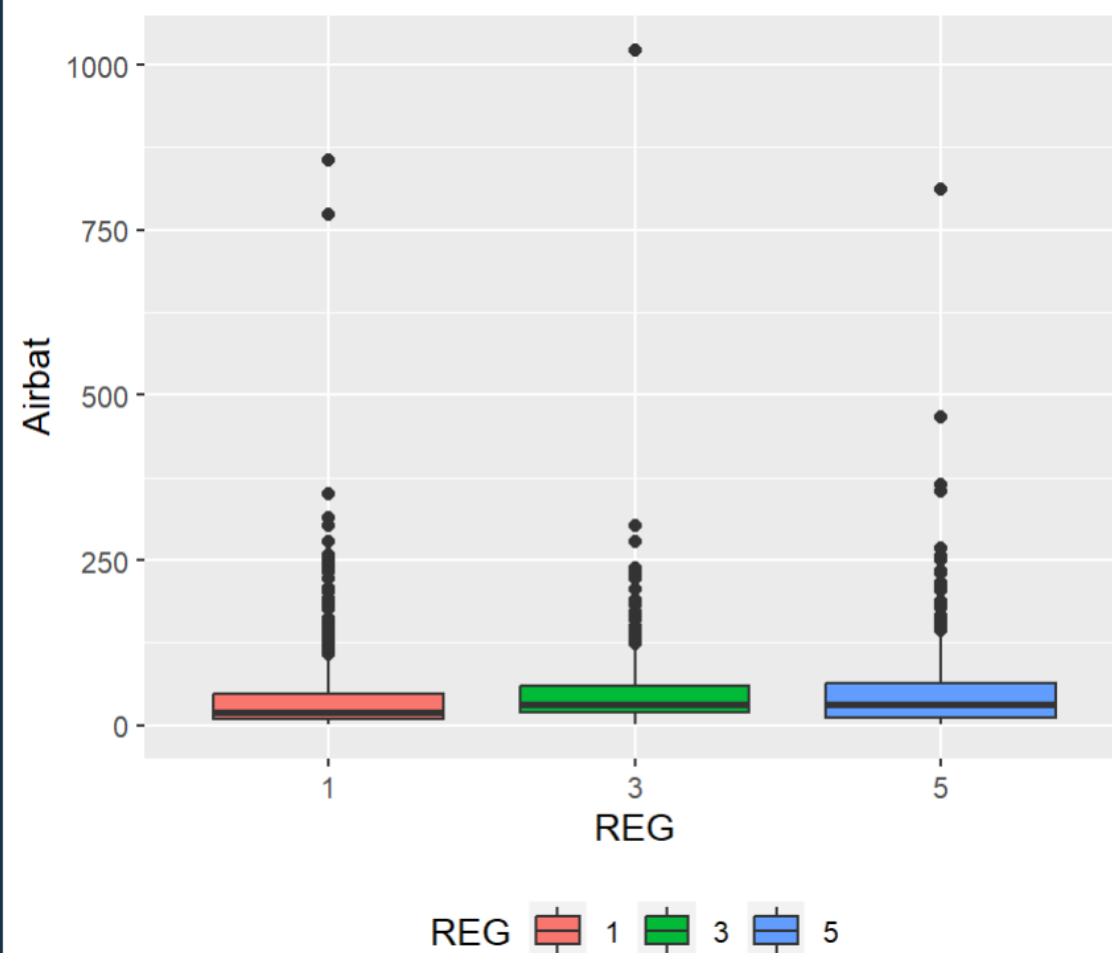
Packages

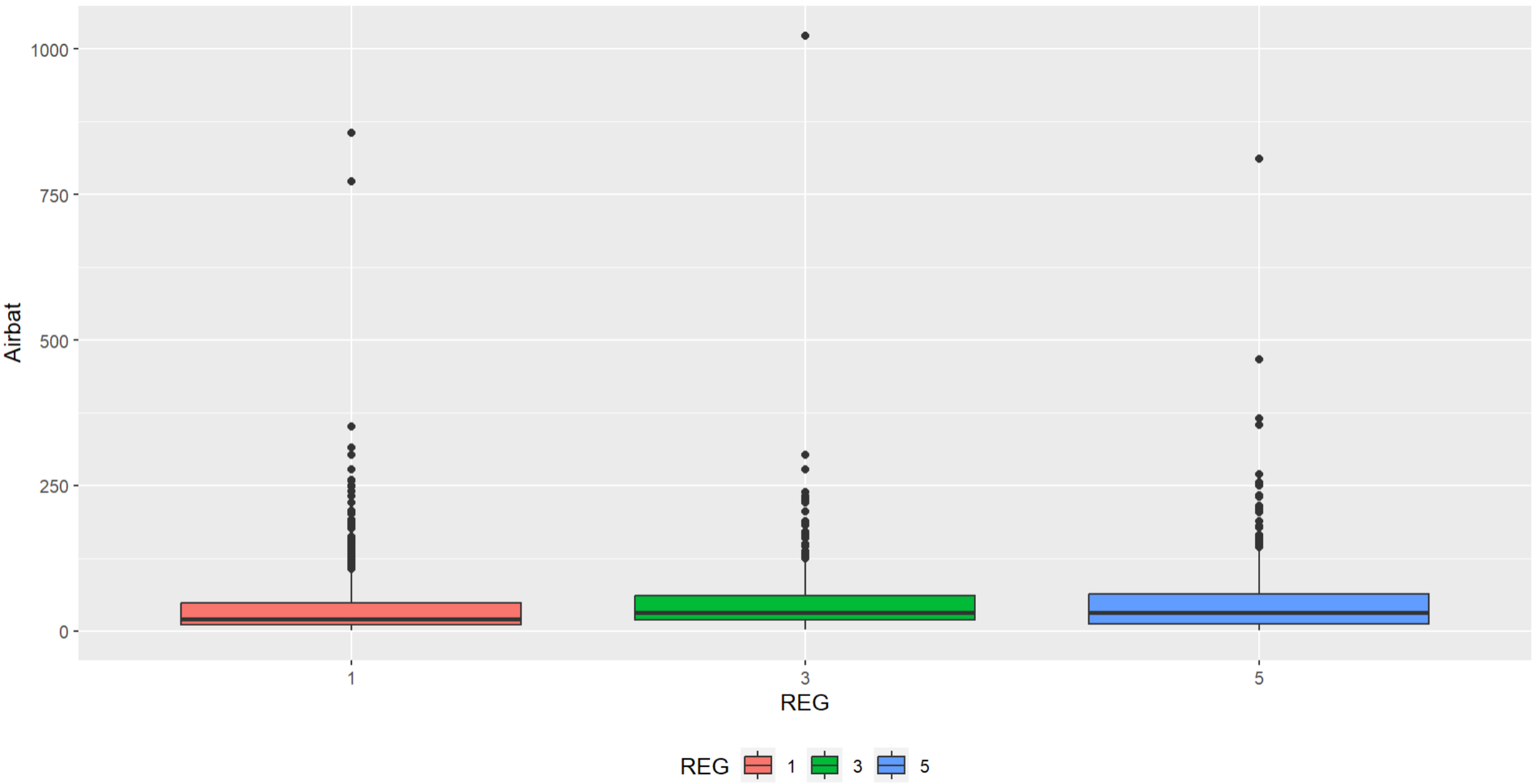
Help

Viewer

Presentation

Zoom Export





```
8 swiss1 <- swissmunicipalities %>% mutate(REG = factor(REG)) # remake REG as a factor
9 cl <- sampling::cluster(data = swiss1, # invoke the cluster function from the package sampling (::)
10     clustertype = "REG",
11     size = 3,
12     method = "srswor",
13     description = TRUE)
14
15 g <- ggplot(swiss1 ) # use ggplot layers to construct plot
16 g <- g + geom_boxplot(aes(x = REG, y = Airbat, fill = REG)) # add boxplot layer
17 g <- g + theme( legend.position = "bottom" ) # add a theme modification
18 g # print the plot object
19 3/7 # proportion of categories selected
20 data <- getdata(swiss1, cl)
21 data2 <- within(data, REG <- factor(REG)) # a different way to reform REG as a factor
22 g <- ggplot(data2, aes(x = REG, y = Airbat, fill = REG))
23 g <- g + geom_boxplot()
24 g <- g + theme( legend.position = "bottom" )
25 g
26
27
28
29
30
31
32
33
```

```
> library(sampling)
> data("swissmunicipalities")
> table(swissmunicipalities$REG)

 1  2  3  4  5  6  7
589 913 321 171 471 186 245
> cl <- sampling::cluster(swissmunicipalities, clustername = "REG", size = 3, method = "srswor", description = TRUE)
Number of selected clusters: 3
Number of units in the population and number of selected units: 2896 978
> head(cl)
  REG ID_unit   Prob
1   3     63 0.4285714
2   3    668 0.4285714
3   3   1507 0.4285714
4   3   1499 0.4285714
5   3   1155 0.4285714
6   3    423 0.4285714
> |
```

# Stratified sampling



Source

Console

Terminal x

Background Jobs x

R 4.1.2 · D:/RPACKAGES/Intro2MVS/

```
> str <- sampler::ssamp(df = swiss1, n = 20, strata = REG)
> str %>% group_by(REG) %>% summarize(n())
# A tibble: 7 x 2
  REG   `n()`
  <fct> <int>
1 1         4
2 2         6
3 3         2
4 4         1
5 5         3
6 6         1
7 7         2
> swiss1 %>% group_by(REG) %>% summarise(nu = n())
# A tibble: 7 x 2
  REG   nu
  <fct> <int>
1 1   589
2 2   913
3 3   321
4 4   171
5 5   471
6 6   186
7 7   245
> |
```

**BIAS**



### **Definition 1.15**


**Selection bias** results when a subset of experimental units in the population have little or no chance of being selected for the sample.

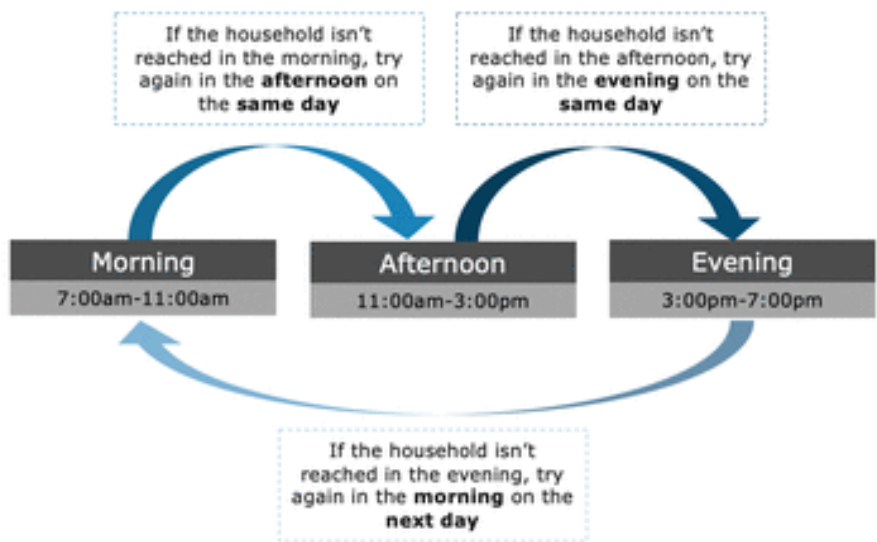
### **Definition 1.16**

**Nonresponse bias** is a type of selection bias that results when data on all experimental units in a sample are not obtained.

### **Definition 1.17**

Intentionally selecting a biased sample in order to produce misleading statistics is considered **unethical statistical practice**.





Try calling back the household in the next time slot for up to **7 attempts**




# Read the examples

## EXAMPLE 1.5

### Method of Data Collection— Study of a Reinforced Concrete Building


As part of a cooperative research agreement between the United States and Japan, a full-scale reinforced concrete building was designed and tested under simulated earthquake conditions in Japan. For one part of the study (published in the *Journal of Structural Engineering*), several U.S. design engineers located on the west coast were asked to evaluate the new design. Of the 48 engineers surveyed, 75% believed the shear wall of the structure to be too lightly reinforced.

- a. Identify the data-collection method.
- b. Identify the target population.
- c. Are the sample data representative of the population?



**Definition 1.17**

**Statistical thinking** involves applying rational thought and the science of statistics to critically assess data and inferences.



MATH 4753 + 4773

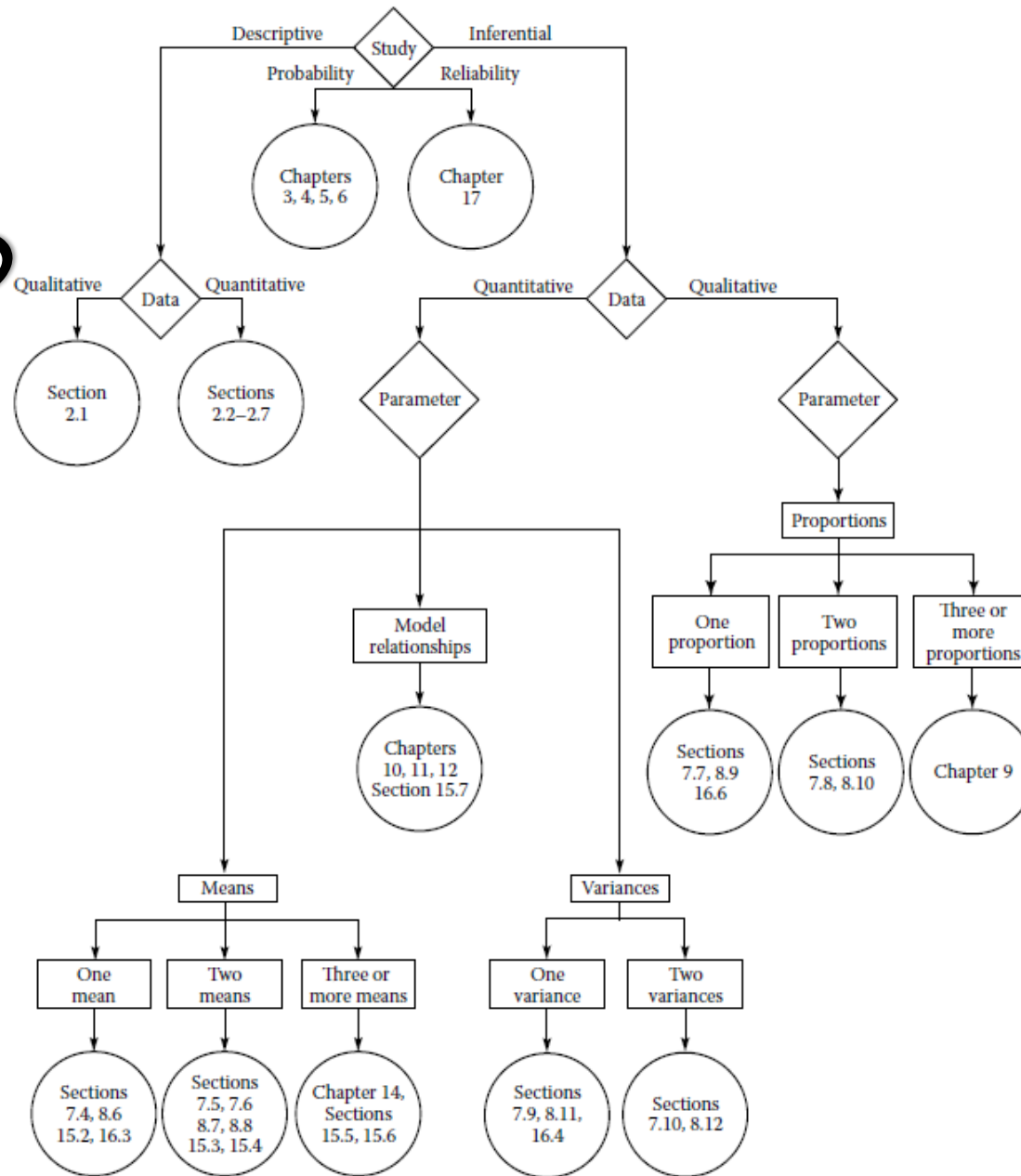


FIGURE 1.3  
Flowchart of statistical methods described in the text

## Quick Review

### Key Terms

Data 2	Measure of reliability 5	Quantitative data 6	Selection bias 13
Descriptive statistics 3	Measurement error 4	Random number generator 9	Simple random sample 9
Designed experiment 8	Nonresponse bias 13	Reliability 4	Statistical thinking 16
Experimental unit 4	Observational study 9	Representative sample 9	Statistics 2
Inference 3	Population 3	Sample 3	Survey 8
Inferential statistics 3	Qualitative data 6		Variable 4

### Chapter Summary Notes

- Two types of statistical applications: *descriptive* and *inferential*
- Fundamental elements of statistics: *population, experimental units, variable, sample, inference, measure of reliability*
- *Descriptive statistics* involves summarizing and describing data sets.
- *Inferential statistics* involves using a sample to make inferences about a population.
- Two types of data: *quantitative* and *qualitative*
- Three data collection methods: **published source, designed experiment, observational study.**
- Types of random sampling: **simple random sample, stratified random sampling, cluster sampling, and systematic sampling.**